

A decent try at all of the problems can earn you 5 points on Exam #3. (Less-than-decent tries earn less than 5 points – my call.) These are due Wednesday, November 7 at the exam.

1. Find the absolute and local maximum and minimum values of the following functions.

- (a) $f(x) = 4x - 1$, $x \leq 8$.
- (b) $f(x) = 2x^3 + 3x^2 + 4$, $-2 \leq x \leq 1$.
- (c) $f(x) = x^2 + 2/x$, $\frac{1}{2} \leq x \leq 2$.
- (d) $f(x) = x^{4/5}$, $-32 \leq x \leq 1$.
- (e) $f(x) = \sin x + \cos x$, $0 \leq x \leq \pi/3$.
- (f) $f(x) = (\ln x)/x^2$, $1 \leq x \leq 3$.

2. Find the critical numbers of

- (a) $f(x) = 4x^3 - 9x^2 - 12x + 3$
- (b) $f(x) = \sqrt[3]{x^2 - x}$
- (c) $f(\theta) = \sin^2(2\theta)$

3. Verify that the function $f(x) = \sqrt{x}$ on the interval $[1, 4]$ satisfies the hypotheses of the Mean Value Theorem. Then find all numbers c that satisfy the conclusion of the Mean Value Theorem.

4. Find the interval(s) on which $y = \frac{x}{(1+x)^2}$ is concave upward.

5. For the following functions, find (a) the intervals of increase or decrease, (b) the local maximum and minimum values, (c) the intervals of concavity, and (d) the x -coordinates of the points of inflection. Then use this information to sketch the graph.

- (a) $f(x) = 1 - 4x + 5x^2 - x^3$
- (b) $g(x) = x + 3x^{2/3}$

6. Sketch the graph of a function that satisfies the following conditions:

$$\begin{aligned} f(0) &= 0, f'(-2) = f'(1) = f'(9) = 0, \\ \lim_{x \rightarrow \infty} f(x) &= 0, \lim_{x \rightarrow 6} f(x) = -\infty, \\ f'(x) &< 0 \text{ on } (-\infty, -2), (1, 6), \text{ and } (9, \infty), \\ f'(x) &> 0 \text{ on } (-2, 1) \text{ and } (6, 9), \\ f''(x) &> 0 \text{ on } (-\infty, 0) \text{ and } (12, \infty), \\ f''(x) &< 0 \text{ on } (0, 6) \text{ and } (6, 12). \end{aligned}$$

7. If 1200 cm² of material is available to make a box with a square base and an open top, find the largest possible volume of the box.

8. Find the point on the parabola $x + y^2 = 0$ that is closest to the point $(0, -3)$.

9. A poster is to have an area of 180 in² with 1-inch margins at the bottom and sides and a 2-inch margin at the top. What dimensions will give the largest printed area?

10. Find the linearization of $f(x) = \sqrt[3]{1+3x}$ at $a = 0$. State the corresponding linear approximation and use it to give an approximate value for $\sqrt[3]{1.03}$.

11. Evaluate dy if $y = x^3 - 2x^2 + 1$, $x = 2$, and $dx = 0.2$.

12. Use differentials to approximate $8 + \sqrt{143.6}$.